

Information Economics

Problem Set 3

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1. A manufacturer produces two competing products, A and B, and wants to sell these products to two groups of customers, groups 1 and 2. Group 1 has 1,000 members and group 2 has 1,500 members. The values each customer places on a unit of these two products are shown in the table below. We use V_{ij} to denote a group- i consumer's valuation for product j . For example, $V_{1,A} = \$10$, $V_{2,A} = \$12$, etc.

	Product A	Product B
Group 1	\$10	\$8
Group 2	\$12	\$15

Each consumer will buy at most one unit of either product A or product B. If a group- i consumer buys product j , her consumer surplus is defined to be $V_{ij} - P_j$, where P_j is the price for product j . One will buy the product intended for her if it results in a nonnegative consumer surplus which is no lower than that of buying the other product. Chandler wants to set prices for each product so that group 1 members purchase product A and group 2 members purchase product B. Chandler can only set ONE price for product A and ONE price for product B. It cannot charge different groups different prices for the same product.

- (a) Formulate the manufacturer's pricing problem for maximizing revenues.
 - (b) Find the optimal prices analytically.
2. Consider a manufacturer-retailer relationship in a supply chain. The manufacturer produces a product at a unit production cost c and sell it to the retailer. The retailer is a newsvendor facing random market demand $D \sim \text{Uni}(0, 1)$. The unit retail price is fixed to r , which is public to everyone. However, the retailer may be either efficient or inefficient: An efficient retailer sells a product with a unit retail cost d_1 while an inefficient one does so with a unit retail cost d_2 , where $d_1 < d_2$. Therefore, the unit "net sales revenues" of an efficient retailer and an inefficient retailer are defined to be $r_H = r - d_1$ and $r_L = r - d_2$. Naturally, $r_L < r_H$. The retailer's retail cost is his private information. The manufacturer believes that the retailer is inefficient with probability β or efficient with probability $1 - \beta$. Each player acts to maximize her/his expected profit. Before the selling season starts, the manufacturer offers the retailer a menu of two contracts, $\{(q_L, t_L), (q_H, t_H)\}$, where (q_i, t_i) is intended for the type- i retailer, $i \in \{L, H\}$. If the retailer selects (q_i, t_i) , he obtains q_i units from the manufacturer by paying t_i . He then faces a typical newsvendor situation with q_i units of inventory at the beginning of the selling season.
 - (a) In our two-type monopoly pricing model, we assumed that the agent's utility function is $v(q, t, \theta) = \theta v(q) - t$, where θ is the agent's type and $v(\cdot)$ is strictly increasing and strictly concave. For the retailer in this problem, what is θ ? What is $v(q)$? Write down the closed-form expression of $v(q)$ as a function of q . Show that it is strictly increasing and strictly concave in the domain of interest.
 - (b) By assuming complete information, find the first-best menu for the two types of retailers.
 - (c) Suppose there is information asymmetry, formulate the manufacturer's contract design problem whose solution is the second-best menu.
 - (d) Continue from Part (c). Suppose $c = 2$, $r_L = 8$, $r_H = 10$, and $\beta = \frac{1}{2}$. Find the manufacturer's second-best menu.

Note. Plugging in numbers into the formula we derived on slides is fine.
 - (e) Continue from Part (d). Show that the low-type order quantity is lower than the high-type order quantity. Then show that the low-type order quantity is lower than the efficient level.