Operations Research, Spring 2016

Pre-lecture Problems for Lecture 6: Linear Programming Duality

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Note. The deadline of submitting the pre-lecture problem is 10:10am, March 31, 2016. Please submit a hard copy of your work in class. Late submissions will not be accepted. Each student must submit her/his individual work. Submit ONLY the problem that counts for grades.

1. (0 point) Find the dual for the following LP:

2. (0 point) Consider a primal LP

$$\begin{array}{ll} \max & 3x_1 + 5x_2 \\ \text{s.t.} & x_1 + x_2 \leq 8 \\ & x_1 + 2x_2 \leq 12 \\ & x_1 \geq 0, x_2 \geq 0. \end{array}$$

- (a) Find a primal optimal solution x^* .
- (b) Formulate the dual LP.
- (c) Solve the dual LP to get a dual optimal solution y^* . Show that $c^Tx^* = (y^*)^Tb$, where c and b are the primal and dual objective function.
- 3. (10 points) Consider the primal LP that you just solved in Problem 2.
 - (a) Find a primal optimal basis B. Verify that $A_B^{-1}b=x_B^*$, the basic variables of the optimal solution x^* you found in Problem 2a.
 - (b) Verify that $c_B^T A_B^{-1} = y^*$, the dual optimal solution you found in Problem 2c.
 - (c) Find the shadow prices for the two primal constraints.¹

¹If you are applying the correct concept, you may need no calculation for finding them. But maybe you would like to do a verification by calculating them by solving two modified primal LPs?