

Operations Research, Spring 2017
Pre-lecture Problems for Lecture 11:
Algorithms for Nonlinear Programming

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Note. The deadline of submitting the pre-lecture problem is **9:20 am, May 11, 2017**. Please submit a hard copy of your work in class. Late submissions will not be accepted. Each student must submit her/his individual work. Submit **ONLY** the problem that counts for grades.

1. (0 point) Let's solve $\min_{x \in \mathbb{R}^2} f(x) = x_1^2 + 2x_2^2$ by gradient descent. In each iteration, let the step size be that bringing you to the global minimum along the improving direction.
 - (a) Find the gradient of $f(x)$.
 - (b) Let $x^0 = (1, 0)$ be the initial solution. Run on iteration of gradient descent to find the next solution x^1 .
 - (c) Starting from x^1 , run one more iteration of gradient descent to find the next solution x^2 .
2. (0 point) Let's solve $\min_{x \in \mathbb{R}^2} f(x) = x_1^2 + 2x_2^3$ by Newton's method.
 - (a) Find the Hessian of $f(x)$.
 - (b) Let $x^0 = (6, 6)$ be the initial solution. Run on iteration of Newton's method to find the next solution x^1 .
 - (c) Starting from x^1 , run one more iteration of Newton's method to find the next solution x^2 .
3. (10 points; 2 points each) Let's solve

$$\min_{x \in \mathbb{R}} f(x) = \frac{1}{4}x^4 - \frac{1}{3}x^3 - x^2 + 4x + 1.$$

Let $x^0 = 1$ be the initial solution.

- (a) Find the gradient and Hessian of $f(x)$.
- (b) Run one iteration of gradient descent to get the next solution x^G . In each iteration, let the step size be that bringing you to the global minimum along the improving direction.
- (c) Run one iteration of Newton's method to get the next solution x^F .