

Operations Research, Spring 2016

Suggested Solution for Pre-lecture Problems for Lecture 5

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1. Let x_{ij} = oz of chemical i for product j , $i = 1, 2, j = 1, 2$.

$$\begin{aligned}
 \max \quad & 6(x_{11} + x_{21}) + 5(x_{12} + x_{22}) - 6(x_{11} + x_{12}) - 4(x_{21} + x_{22}) \\
 \text{s.t.} \quad & x_{11} \geq 0.6(x_{11} + x_{21}) \\
 & x_{22} \geq 0.5(x_{12} + x_{22}) \\
 & x_{11} + x_{21} \leq 100 \\
 & x_{12} + x_{22} \leq 90 \\
 & x_{11} + x_{12} \leq 130 \\
 & x_{21} + x_{22} \leq 80 \\
 & x_{ij} \geq 0 \quad \forall i = 1, 2, j = 1, 2.
 \end{aligned}$$

2. The linearized LP is

$$\begin{aligned}
 \max \quad & 5w + 3x_2 \\
 \text{s.t.} \quad & w \leq x_1 \\
 & w \leq x_2 \\
 & x_1 \leq 16 \\
 & x_2 \leq 16 \\
 & x_1 + 4x_2 \leq 20 \\
 & x_2 \geq 8 \\
 & x_i \geq 0 \quad \forall i = 1, 2.
 \end{aligned}$$

3. The linearized LP is

$$\begin{aligned}
 \max \quad & 5s - 3t \\
 \text{s.t.} \quad & s \leq x_1 \\
 & s \leq x_2 \\
 & t \geq x_2 \\
 & t \geq x_1 + x_3 \\
 & x_1 + u \geq v + w \\
 & u \leq x_1 \\
 & u \leq x_2 + 4 \\
 & v \geq 16 - x_1 \\
 & v \geq x_1 - 16 \\
 & w \geq x_1 \\
 & w \geq 4x_2 - x_3 \\
 & x_i \geq 0 \quad \forall i = 1, 2, 3.
 \end{aligned}$$