Homework Assignment #4

Note

This assignment is due 2:10PM Tuesday, April 1, 2014. Please write or type your answers on A4 (or similar size) paper. Drop your homework by the due time in Yih-Kuen Tsay's mail box on the first floor of Management College Building II. Late submission will be penalized by 20% for each working day overdue. You may discuss the problems with others, but copying answers is strictly forbidden.

Problems

There are five problems in this assignment, each accounting for 20 points. (Note: problems marked with "(X.XX)" are taken from [Manber 1989] with probable adaptation.)

1. (5.7) Write a program (or modify the code discussed in class) to recover the solution to a knapsack problem using the *belong* flag. You should make your solution as efficient as possible.

2. (5.8) In algorithm *Knapsack*, we first checked whether the ith item is unnecessary (by checking $P[i-1, j]$). If there is a solution with the $i-1$ items, we take this solution. We can also make the opposite choice, which is to take the solution with the ith item if it exists (i.e., check $P[i-1, j-k_i]$ first). Which version do you think will have a better performance? Redraw Fig. 5.11 (see notes/slides) to reflect this choice.

3. (5.20) Let x_1, x_2, …, x_n be a set of integers, and let $S = \sum_{i=1}^{n} x_i$. Design an algorithm to partition the set into two subsets of equal sum, or determine that it is impossible to do so. The algorithm should run in time $O(nS)$.

4. (5.22) In the **towers of Hanoi** puzzle, there are three pegs A, B, and C, with n (generalizing the original eight) disks of different sizes stacked in decreasing order on peg A. The objective is to transfer all the disks on peg A to peg B, moving one disk at a time (from one peg to one of the other two) and never having a larger disk stacked upon a smaller one.

   (a) Give an algorithm to solve the puzzle. Explain how induction works here.

   (b) Compute the total number of moves in the algorithm. Show the details of your calculation.

5. (5.23) Write a non-recursive program (in suitable pseudocode) that prints the moves of the solution to the towers of Hanoi puzzle.