# Algorithms 2023: Introduction

(Based on [Manber 1989])

Yih-Kuen Tsay

September 5, 2023

## 1 About Algorithms

## What They Are

- An algorithm is, broadly speaking, a step-by-step procedure for solving a problem or accomplishing some end.
- When it is meant for the computer, each step in an algorithm should be realizable by well-defined, limited primitive operations that the computer understands.
- You actually have learned several algorithms during your school years. Can you name one?
  - /\* Euclid's algorithm and Gaussian elimination are probably the most notable. \*/
- Algorithm design is an important and usually the hardest part of programming (which consists in finding/devising a solution and translating it into a computer program).
- Better algorithms (designed once, used forever) save more time and money.

### Development of an Algorithm

- We typically are given a problem statement, including input and output requirements, that is an abstract yet *accurate* and *precise* account of the problem to be solved and the properties of a satisfactory solution.
- The development of an algorithm involves the following tasks:
  - 1. Design (main subject of this course)
  - 2. Verification (or Proof of Correctness)
    - /\* The methods of verification include testing, formal verification, etc. \*/
  - 3. Analysis
  - 4. Implementation

(May need to iterate.)

#### **Main Concerns**

- Why is algorithm design difficult?
  - Computers are different from humans; they are very fast and can handle much larger amounts of data.
  - Counterintuitive approaches may be needed, because of large problem scales.
    - /\* Intuitive algorithms that work well for small problem instances may be terrible for large problem instances. \*/
  - Better solutions, if worthwhile (with greater payoffs), may be more complicated.
- How do we approach it?

## 2 Our Emphasis

### A Creative Approach to the Subject

- Emphasis of the creative side
  - not only memorizing solutions
  - but also learning to create by trying to create
- Induction as one central design method
  - to explain/understand the principles behind a design
  - to systematically guide the creation process

## Design by Induction

- Design by induction draws analogies from proving theorems by mathematical induction.
- In a proof by induction, we do not prove a statement from scratch, but rather we show
  - 1. the correctness of the statement follows from that of the same statement for smaller instances and
  - 2. the correctness of the statement for a small base case.
- This suggests an approach to algorithm design that concentrates on *extending* solutions for smaller problem instances to solutions for larger ones.
- Induction may not solve every problem, but is very helpful.
  - /\* Some types of problems require essentially trying all possibilities, e.g., the  $2^n$  possible truth assignments to n Boolean variables. One may still enumerate all the possibilities in terms of induction, but that does not really help get a more efficient solution.\*/