







# Compositional Specification and Reasoning

Yih-Kuen Tsay

Dept. of Information Management  
National Taiwan University

# Outline

-  Review of the Owicki-Gries Method
-  Compositional Methods
-  The Mutual Induction Mechanism
-  Compositional Reasoning in Temporal Logic
-  Interface Automata
-  Concluding Remarks




# Sequential vs. Concurrent Programs/Components

- Both generate computations, which are sequences of states possibly with labels on the steps:  $s_0 \xrightarrow{l_1} s_1 \xrightarrow{l_2} \dots \xrightarrow{l_n} s_n$   
( $\xrightarrow{l_{n+1}} s_{n+1} \xrightarrow{l_{n+2}} \dots$ ).
- For a sequential component, only its **start** and **final** states matter to other components.
- Computations of a concurrent component are produced by *interleaving its steps with those of an 'arbitrary but compatible' environment*.
- Many interesting concurrent components, often referred to as *reactive* components, are not meant to terminate.

# Taking Interference into Account

Probably the first and best-known attempt at generalizing Hoare Logic to concurrent programs is:

*Owicki, S. and Gries, D. An axiomatic proof technique for parallel programs. Acta Informatica, 6:319-340, 1976.*

-  Proof outlines (for terminating programs)
-  Interference freedom (here, one can sense the notion of “assume-guarantee”)
-  Auxiliary variables

# Interference Freedom

- 🌐 A proof outline  $\{p_i\} S_i^* \{q_i\}$  *does not interfere* with another proof outline  $\{p_j\} S_j^* \{q_j\}$  if the following holds:  
*For every normal assignment or atomic region  $R$  in  $S_i$  and every assertion  $r$  in  $\{p_j\} S_j^* \{q_j\}$ ,*

$$\{r \wedge \text{pre}(R)\} R \{r\}.$$

- 🌐 Given a parallel program  $[S_1 \parallel \dots \parallel S_n]$ , the proof outlines  $\{p_i\} S_i^* \{q_i\}$ ,  $1 \leq i \leq n$ , are said to be *interference free* if none of the proof outlines interferes with any other.

# Main Composition Rule of Owicki and Gries

$$\frac{\{p_i\} S_i^* \{q_i\}, 1 \leq i \leq n, \text{ are interference free}}{\{\bigwedge_{i=1}^n p_i\} [S_1 \parallel \cdots \parallel S_n] \{\bigwedge_{i=1}^n q_i\}}$$

# Criteria of Compositionality

- 🌐 Compositional specifications of a component should not refer to the **internal structures** of itself and/or other components.
- 🌐 This is desirable, as we often want to speak of replacing a component by another that satisfies the same specification.
- 🌐 So, the purists would say, “Owicki and Greis’ method does not qualify as a compositional method.”

Remark: Owicki and Greis’ method (or its adaptation) is probably the most usable when one has at hand all the code of a (small) concurrent system.

# Lamport's 'Hoare Logic'

In this probably forgotten paper, Lamport proposed a new interpretation to pre and post-conditions:

*Lamport, L. The 'Hoare Logic' of concurrent programs. Acta Informatica, 14:21-37, 1980.*

- 🌐 Notation:  $\{P\} S \{Q\}$   
Meaning: If execution starts *anywhere* in  $S$  with  $P$  true, then executing  $S$  (1) will leave  $P$  true while control is in  $S$  and (2) if terminating, will make  $Q$  true.
- 🌐 The usual Hoare triple would be expressed as  $\{P\} \langle S \rangle \{Q\}$ , where  $\langle \cdot \rangle$  indicates atomic execution.



# Lamport's 'Hoare Logic' (cont.)

- 🌐 Rule of consequence (can't strengthen the pre-condition):

$$\frac{\{P\} S \{Q'\}, Q' \rightarrow Q}{\{P\} S \{Q\}}$$

- 🌐 Rules of Conjunction and Disjunction:

$$\frac{\{P\} S \{Q\}, \{P'\} S \{Q'\}}{\{P \wedge P'\} S \{Q \wedge Q'\}} \quad \frac{\{P\} S \{Q\}, \{P'\} S \{Q'\}}{\{P \vee P'\} S \{Q \vee Q'\}}$$

# Lamport's 'Hoare Logic' (cont.)

🌐 Rule of Sequential Composition:

$$\frac{\{P\} S \{Q\}, \{R\} T \{U\}, Q \wedge at(T) \rightarrow R}{\{(in(S) \rightarrow P) \wedge (in(T) \rightarrow R)\} S; T \{U\}}$$

🌐 Rule of Parallel Composition:

$$\frac{\{P\} S_i \{P\}, 1 \leq i \leq n}{\{P\} \mathbf{cobegin} \parallel_{i=1}^n S_i \mathbf{coend} \{P\}}$$

# UNITY Logic

UNITY was once quite popular. Its logic has been modified in a subsequent work.

*Misra, J. A logic for concurrent programming. Journal of Computer and Software Engineering, 3(2): 239-272, 1995.*

- 🌐 A program consists of (1) an **initial condition** and (2) a **set of actions** (or conditional multiple-assignments), which always includes **skip**.
- 🌐 Main Notation:  $p \text{ co } q \triangleq \forall s :: \{p\} s \{q\}$  (over all action  $s$  of a given program).

Note: There are also operators for liveness properties.

# UNITY Logic (cont.)

- 🌐 Notation:  $p \text{ co } q \triangleq \forall s :: \{p\} s \{q\}$  ( $p$  constrains  $q$ )
- 🌐 Meaning: Whenever  $p$  holds,  $q$  holds after the execution of any single action (if it terminates).
- 🌐 Examples:
  - ☀️ “ $\forall m :: x = m \text{ co } x \geq m$ ” says  $x$  never decreases.
  - ☀️ “ $\forall m, n :: x, y = m, n \text{ co } x = m \vee y = n$ ” says  $x$  and  $y$  never change simultaneously.

# UNITY Logic vs. 'Hoare Logic'

- 🌐 “co” enjoys the complete rule of consequence.
- 🌐 Rules of conjunction and disjunction also hold.
- 🌐 Stronger rule of parallel composition:

$$\frac{p \text{ co } q \text{ in } F, p \text{ co } q \text{ in } G}{p \text{ co } q \text{ in } F \parallel G}$$

- 🌐 But, “co” is much less convenient for sequential composition.

# Jones' Rely/Guarantee Pairs

*Jones, C.B. Tentative steps towards a development method for interfering programs. TOPLAS, 5(4):596-619, 1983.*

- 🌐 Assumption about the environment is expressed by a pre-condition and a *rely*-condition
- 🌐 Promised behavior of a component is expressed by a post-condition and a *guarantee*-condition.
- 🌐 Both rely and guarantee-conditions are **predicates of two states**, to deal with reactive behavior.

*We will illustrate rely and guarantee-conditions in the context of temporal logic.*

# Assume-Guarantee Specifications

- 🌐 A component will behave properly only if its environment (the context where it is used) does.
- 🌐 To summarize the lessons learned, the specification of a component should include
  1. **assumed** properties about its environment and
  2. **guaranteed** properties of the module if the environment obeys the assumption.
- 🌐 The names vary: rely-guarantee, assumption-commitment, assumption-guarantee, etc.

Note: we will focus on reactive behavior from now on.

# Mutual Dependency

Let  $A \triangleright G$  denote a generic component specification with assumption  $A$  and guarantee  $G$ .

The following composition rule looks plausible, but is circular and unsound without an adequate semantics for  $\triangleright$ .

$$\frac{\begin{array}{l} \llbracket M_1 \rrbracket \models A_1 \triangleright G_1 \\ \llbracket M_2 \rrbracket \models A_2 \triangleright G_2 \\ A \wedge G_1 \rightarrow A_2 \\ A \wedge G_2 \rightarrow A_1 \end{array}}{\llbracket M_1 \parallel M_2 \rrbracket \models A \triangleright (G_1 \wedge G_2)}$$

The circularity may be broken by introducing a mutual induction mechanism into  $\triangleright$ .



# The Mutual Induction Mechanism

The mechanism was probably first proposed in

*Misra, J. and Chandy, K. Proofs of networks of processes. IEEE Transactions on Software Engineering, 7:417–426, 1981.*

- 🌐 Notation:  $r \mid h \mid s$ 
  - ☀️  $h$  is a CSP-like process with message communication.
  - ☀️  $r$  and  $s$  are assertions on the *traces* of  $h$
- 🌐 Meaning: (1)  $s$  holds initially and (2) if  $r$  holds up to the  $k$ -th point in a trace of  $h$ , then  $s$  holds up to the  $(k + 1)$ -th point in that trace, for all  $k$ .

Note: “ $r[h]s$ ” is used if  $r$  or  $s$  also refers to the internal communication channels of  $h$ .

# Misra and Chandy's Proof System

🌐 Rule of network composition:

$$\frac{r_i \mid h_i \mid s_i, 1 \leq i \leq n}{\left(\bigwedge_{i=1}^n r_i\right) \left[ \parallel_{i=1}^n h_i \right] \left(\bigwedge_{i=1}^n s_i\right)}$$

🌐 Rule of inductive consequence:

$$\frac{(s \wedge r) \rightarrow r'; r' \mid h \mid s}{r \mid h \mid s} \quad \frac{r \mid h \mid s'; s' \rightarrow s}{r \mid h \mid s}$$

🌐 Theorem of Hierarchy:

$$\frac{r_i \mid h_i \mid s_i, 1 \leq i \leq n; \left( \bigwedge_{i=1}^n s_i \wedge R_0 \right) \rightarrow \bigwedge_{i=1}^n r_i; \bigwedge_{i=1}^n s_i \rightarrow S_0}{R_0 \mid \prod_{i=1}^n h_i \mid S_0}$$

There are also rules for proving “ $r \mid h \mid s$ ” from scratch.

- 🌐 Induction on the length of computation works for safety properties (invariants).
- 🌐 But, it does not for liveness, which needs explicit well-founded induction (by defining variant functions that decrease as computation progresses)

*Pnueli, A. In transition from global to modular temporal reasoning about programs. Logics and Models of Concurrent Systems, 123-144. Springer, 1985.*

- 🌐 Steps by the component and those by its environment need to be distinguished.
- 🌐 Induction structures are required.
- 🌐 Computations of a component allow arbitrary environment steps
- 🌐 Past temporal operators (as an alternative to history variables) are useful.
- 🌐 Barringer and Kuiper had explored some of the above ideas earlier [LNCS 197, 1984].

# Conditions for Easy Compositionality

- Exactly one single component is accountable for changes at the interface in each step.
- Input-enabled**: a component is always ready to perform any input action (which is paired with some output action from the environment).
  - For shared-variable models, this is automatically true.
- With these conditions,  $\llbracket C_1 \parallel C_2 \rrbracket$  can be easily understood as  $\llbracket C_1 \rrbracket \cap \llbracket C_2 \rrbracket$ .

# Modular Reasoning in TLA

The probably most-cited work of assume-guarantee specification in temporal logic is:

*Abadi, M. and Lamport, L. Conjoining specifications. TOPLAS, 17(3):507-534, 1995.*

- 🌐 Main notation:  $E \overset{+}{\triangleright} M$   
Meaning: (1)  $M$  holds initially and (2) for  $n \geq 0$ , if  $E$  holds for the prefix of length  $n$  in a computation, then  $M$  holds for the prefix of length  $n + 1$ .
- 🌐 TLA is extended in some sense.
- 🌐 Liveness properties are treated.

# Abadi and Lamport

🌐 Three kinds of implication (between safety properties  $A$  and  $G$ ):

☀️  $A \rightarrow G$

$\sigma \models A \rightarrow G \iff \sigma \models A \text{ implies } \sigma \models G.$

☀️  $A \rightarrow\triangleright G$

$\sigma \models A \rightarrow\triangleright G \iff \text{for all } i \geq 0, \sigma|_i \models A \text{ implies } \sigma|_i \models G.$

☀️  $A \overset{+}{\rightarrow}\triangleright G$

$\sigma \models A \overset{+}{\rightarrow}\triangleright G \iff \text{for all } i \geq 0, \sigma|_i \models A \text{ implies } \sigma|_{i+1} \models G.$

🌐 Fundamental relationships

☀️  $A \overset{+}{\rightarrow}\triangleright G$  is the “realizable part” of  $A \rightarrow G$ .

☀️  $M \parallel A \models G \text{ iff } M \models A \rightarrow\triangleright G.$

☀️  $\models A \overset{+}{\rightarrow}\triangleright G = (G \rightarrow\triangleright A) \rightarrow\triangleright G.$

☀️ When  $A$  and  $G$  are “orthogonal”,  $\models A \overset{+}{\rightarrow}\triangleright G = A \rightarrow\triangleright G$  and hence  $M \parallel A \models G \text{ iff } M \models A \overset{+}{\rightarrow}\triangleright G.$



# Abadi and Lamport (cont.)

One of the composition rules:

$$\begin{array}{l}
\vdash A \wedge G_2 \rightarrow A_1 \\
\vdash A \wedge G_1 \rightarrow A_2 \\
\vdash A \wedge G_1 \wedge G_2 \rightarrow G \\
\hline
\vdash (A_1 \xrightarrow{+} G_1) \wedge (A_2 \xrightarrow{+} G_2) \rightarrow (A \xrightarrow{+} G)
\end{array}$$

Alternative form:

$$\begin{array}{l}
M_1 \parallel A_1 \vdash G_1 \\
M_2 \parallel A_2 \vdash G_2 \\
\vdash A \wedge G_2 \rightarrow A_1 \\
\vdash A \wedge G_1 \rightarrow A_2 \\
\vdash A \wedge G_1 \wedge G_2 \rightarrow G \\
\hline
(M_1 \parallel M_2) \parallel A \vdash G
\end{array}$$

# Modular Reasoning in LTL






The operators  $\rightarrow$  and  $\overset{+}{\rightarrow}$  can be formalized in LTL:

*Jonsson, B. and Tsay, Y.-K. Assumption/guarantee specifications in linear-time temporal logic. Theoretical Computer Science, 167:47-72, 1996.*

- 🌐 It makes good use of past temporal operators.
- 🌐 Proof rules are purely syntactical in LTL.

Note: We will omit the treatment of hiding and liveness.



An LTL formula is interpreted over an infinite sequence of states  $\sigma = s_0, s_1, s_2, \dots, s_i, \dots$  relative to a position.

-  State formulae:  $(\sigma, i) \models \varphi$  iff  $\varphi$  holds at  $s_i$ .
-   $(\sigma, i) \models \bigcirc\varphi$  (“next  $\varphi$ ”) iff  $(\sigma, i + 1) \models \varphi$ .
-   $(\sigma, i) \models \Box\varphi$  (“henceforth  $\varphi$ ”) iff  $\forall k \geq i : (\sigma, k) \models \varphi$ .
-   $(\sigma, i) \models \ominus\varphi$  (“before  $\varphi$ ”) iff  $(i > 0) \rightarrow ((\sigma, i - 1) \models \varphi)$ .
-   $(\sigma, i) \models \boxminus\varphi$  (“so-far  $\varphi$ ”) iff  $\forall k : 0 \leq k \leq i : (\sigma, k) \models \varphi$ .

$\neg\varphi, \varphi_1 \wedge \varphi_2, \varphi_1 \vee \varphi_2, \varphi_1 \rightarrow \varphi_2, \dots$ , etc. are defined in the obvious way. We will not use  $\diamond$  or  $\lozenge$  in this talk.

# LTL (cont.)

Syntactic sugars:

-   $u^-$  denotes the value of  $u$  in the previous state; by convention,  $u^-$  equals  $u$  at position 0.
-   $first \triangleq \ominus false$ , which holds only at position 0.

A sequence  $\sigma$  is *satisfies* a temporal formula  $\varphi$  if  $(\sigma, 0) \models \varphi$ .

A formula  $\varphi$  is *valid*, denoted  $\models \varphi$ , if  $\varphi$  is satisfied by every sequence.

# Program keep-ahead

**local**  $a, b : \text{integer}$  **where**  $a = b = 0$

$$P_a :: \left[ \begin{array}{l} \text{loop forever do} \\ [ a := b + 1 ] \end{array} \right] \parallel P_b :: \left[ \begin{array}{l} \text{loop forever do} \\ [ b := a + 1 ] \end{array} \right]$$

$$(a = 0) \wedge (b = 0) \wedge \square \left( \begin{array}{l} (a = b^- + 1) \wedge (b = b^-) \\ \vee (b = a^- + 1) \wedge (a = a^-) \\ \vee (a = a^-) \wedge (b = b^-) \end{array} \right)$$

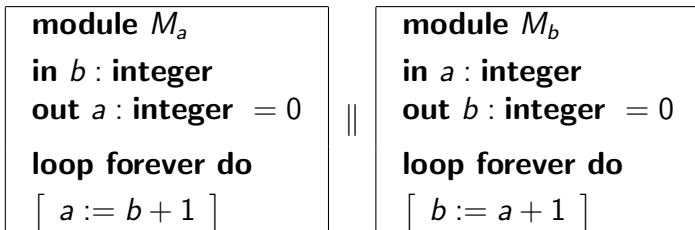
# Program keep-ahead(cont.)

**local**  $a, b : \text{integer where } a = b = 0$

$$P_a :: \left[ \begin{array}{l} \text{loop forever do} \\ [ a := b + 1 ] \end{array} \right] \parallel P_b :: \left[ \begin{array}{l} \text{loop forever do} \\ [ b := a + 1 ] \end{array} \right]$$

$$\square \left( (first \rightarrow (a = 0) \wedge (b = 0)) \wedge \left( \begin{array}{l} \vee (a = b^- + 1) \wedge (b = b^-) \\ \vee (b = a^- + 1) \wedge (a = a^-) \\ \vee (a = a^-) \wedge (b = b^-) \end{array} \right) \right)$$

# Modularized Program keep-ahead



# Modularized Program keep-ahead (cont.)

$$\Phi_{M_a} \stackrel{\Delta}{=} (a = 0) \wedge \square \left( \begin{array}{l} (a = b^- + 1) \wedge (b = b^-) \\ \vee \\ (a = a^-) \end{array} \right)$$

$$\Phi_{M_b} \stackrel{\Delta}{=} (b = 0) \wedge \square \left( \begin{array}{l} (b = a^- + 1) \wedge (a = a^-) \\ \vee \\ (b = b^-) \end{array} \right)$$



# Parallel Composition as Conjunction

- 🌐 The parallel composition of modules  $M_a$  and  $M_b$  is equivalent to Program KEEP-AHEAD; formally,

$$\Phi_{M_a} \wedge \Phi_{M_b} \leftrightarrow \Phi_{\text{KEEP-AHEAD}} .$$

- 🌐 Let  $\Phi_M$  denote the system specification of a module  $M$ . We take  $\Phi_M \rightarrow \varphi$  as the formal definition of the fact that  $M$  satisfies  $\varphi$ , also denoted as  $M \models \varphi$ .
- 🌐 If  $M$  is a module of system  $S$  (i.e.,  $S \equiv M \wedge M'$ , for some  $M'$ ), then  $M \models \varphi$  implies  $S \models \varphi$ .

# Assume-Guarantee Formulae

- Assume that the assumption and the guarantee are safety formulae respectively of the forms  $\Box H_A$  and  $\Box H_G$ , where  $H_A$  and  $H_G$  are past formulae (containing no future temporal operators).
- An A-G formula is defined as follows:

$$\Box H_A \triangleright \Box H_G \stackrel{\Delta}{=} \Box (\ominus \Box H_A \rightarrow \Box H_G)$$

or equivalently,

$$\Box H_A \triangleright \Box H_G \stackrel{\Delta}{=} \Box (\ominus \Box H_A \rightarrow H_G).$$

- Note 1:  $\Box H_A \triangleright \Box H_G$  implies  $H_G$  holds initially (at position 0).
- Note 2:  $(\text{true} \triangleright \Box H_G) \equiv \Box H_G$ .

# Refinement

## Refinement of Guarantee

$$\frac{\Box[\neg \Box H_A \wedge \Box H_{G'} \rightarrow \Box H_G]}{\Box(\neg \Box H_A \rightarrow \Box H_{G'}) \rightarrow \Box(\neg \Box H_A \rightarrow \Box H_G)}$$

## Refinement of Assumption

$$\frac{\Box[\Box H_A \wedge \Box H_A \rightarrow \Box H_{A'}]}{\Box(\neg \Box H_{A'} \rightarrow \Box H_G) \rightarrow \Box(\neg \Box H_A \rightarrow \Box H_G)}$$

$$\models (\Box H_{G_1} \triangleright \Box H_{G_2}) \wedge (\Box H_{G_2} \triangleright \Box H_{G_1}) \rightarrow \Box H_{G_1} \wedge \Box H_{G_2}.$$

This shows that A-G formulae have a **mutual induction** mechanism built in and hence permit “circular reasoning” (mutual dependency).

# Composing A-G Specifications (cont.)

Suppose that  $\Box H_{A_i}$  and  $\Box H_{G_i}$ , for  $1 \leq i \leq n$ ,  $\Box H_A$ , and  $\Box H_G$  are safety formulae.

$$1. \models \Box \left( \Box H_A \wedge \Box \bigwedge_{i=1}^n H_{G_i} \rightarrow H_{A_j} \right), \text{ for } 1 \leq j \leq n$$

$$2. \models \Box \left( \ominus \Box H_A \wedge \Box \bigwedge_{i=1}^n H_{G_i} \rightarrow H_G \right)$$

---


$$\models \bigwedge_{i=1}^n (\Box H_{A_i} \triangleright \Box H_{G_i}) \rightarrow (\Box H_A \triangleright \Box H_G)$$

# A Compositional Verification Rule

Rule MOD-S:

Suppose that  $A_i$ ,  $G_i$ , and  $G$  are canonical safety formulas. Then,

$$\frac{\begin{array}{l} \llbracket M_i \rrbracket \models A_i \triangleright G_i \text{ for } 1 \leq i \leq n \\ \bigwedge_{i=1}^n (A_i \triangleright G_i) \rightarrow G \end{array}}{\llbracket \parallel_{i=1}^n M_i \rrbracket \models G}$$

# Interface Automata

Introduced, studied, and extended in a recent burst of papers by de Alfaro, Henzinger, etc. A good starter:

*de Alfaro, L. Game Models for Open Systems. Verification: Theory and Practice, LNCS 2772, 269-289. Springer, 2003.*

- 🌐 A process language in the form of an automaton with joint actions (divided into inputs and outputs) for specifying the abstract behaviors of a module.
- 🌐 Unreadiness to offer an input in a state is seen as assuming that the environment does not offer the corresponding output in the same state.
- 🌐 So, one single interface automaton describes the input assumption and the output guarantee of a module.

# Interface Automata (cont.)

- 🌐 When two interface automata are composed, an *incompatible* state may result, where some output is enabled in one automaton but the corresponding input is not in the other automaton.
- 🌐 Main decision problem: **compatibility**.  
Two interface automata are *compatible* if there exists an environment in which their product can be useful, i.e., all incompatible states may be avoided.



# Concluding Remarks

- 🌐 Assume-guarantee specification and reasoning were motivated by practical concerns.
- 🌐 The effort had mostly been on obtaining the right form of specifications to enable compositional reasoning.
- 🌐 Advancing the practice seems a lot harder than advancing the theory.
- 🌐 It took over three decades for pre and post-conditions and state invariants to get gradually accepted in practice.
- 🌐 Hopefully, more general assume-guarantee specifications will start to play a complementary role soon.

# References

- Abadi, M. and Lamport, L. Composing specifications. *TOPLAS*, 15(1):73–132, January, 1993.
- Abadi, M. and Lamport, L. Conjoining specifications. *TOPLAS*, 17(3):507–534, May, 1995.
- Abadi, M. and Plotkin, G.D. An abstract account of composition. *MFCS 1995*, 499–508.
- Abadi, M. and Merz, S. A logical view of composition. *TCS*, 114(1):3–30, June, 1993.
- de Alfaro, L. Game Models for Open Systems. *Verification: Theory and Practice, LNCS 2772*, 269–289. Springer, 2003.
- Apt, K.R. and Olderog, E.-R. *Verification of Sequential and Concurrent Programs*, Third Extended Edition, Springer-Verlag, 209.

## References (cont.)

- Collette, P. An explanatory presentation of composition rules for assumption-commitment specifications. *IPL*, 50:31–35, 1994.
- Floyd, R.W. Assigning meanings to programs. *MACS*, 19–32, 1967.
- Hoare, C.A.R. An axiomatic basis for computer programs. *CACM*, 12(10):576–580, May, 1969.
- Jones, C.B. Tentative steps towards a development method for interfering programs. *TOPLAS*, 5(4):596-619, 1983.
- Jonsson, B. and Tsay, Y.-K. Assumption/guarantee specifications in linear-time temporal logic. *TCS*, 167:47–72, October, 1996.
- Lamport, L. The ‘Hoare Logic’ of concurrent programs. *Acta Informatica*, 14:21–37, 1980.

## References (cont.)

- 🌐 Misra, J. A logic for concurrent programming. *Journal of Computer and Software Engineering*, 3(2): 239-272, 1995.
- 🌐 Misra, J. and Chandy, K. Proofs of networks of processes. *IEEE Transactions on Software Engineering*, 7:417-426, 1981.
- 🌐 Owicki, S. and Gries, D. An axiomatic proof technique for parallel programs I. *Acta Informatica*, 6:319-340, 1976.
- 🌐 Pnueli, A. In transition from global to modular temporal reasoning about programs. *Logics and Models of Concurrent Systems*, 123-144. Springer, 1985.