

Homework Assignment #3

Due Time/Date

This assignment is due 2:20PM Tuesday, March 23, 2021. Late submission will be penalized by 20% for each working day overdue.

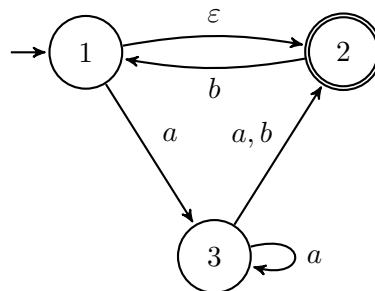
Note

Please write or type your answers on A4 (or similar size) paper. Drop your homework by the due time in Yih-Kuen Tsay's mail box on the first floor of Management College Building 2, or put it on the instructor's desk before the class on the due date starts. You may discuss the problems with others, but copying answers is strictly forbidden.

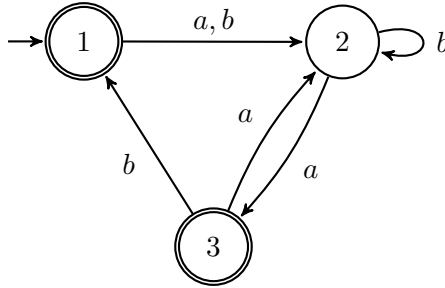
Problems

(Note: problems marked with "Exercise X.XX" or "Problem X.XX" are taken from [Sipser 2013] with probable adaptation.)

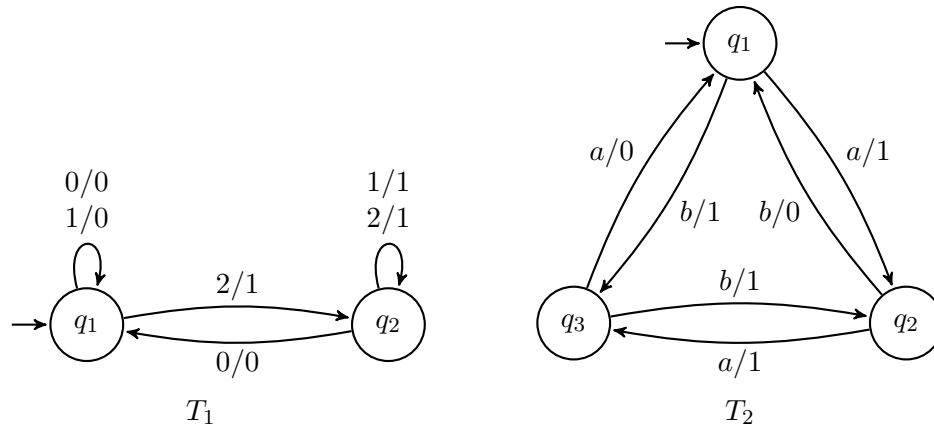
- (Exercise 1.7; 10 points) For each of the following languages, give the state diagram of an NFA, with the specified number of states, that recognizes the language. In all parts, the alphabet is $\{0, 1\}$.
 - The language $\{w \mid w \text{ contains the substring } 1101, \text{ i.e., } w = x1101y \text{ for some } x \text{ and } y\}$ with five states
 - The language $1^+0^*1^*$ with three states
- (Exercise 1.14; 10 points) Show by giving an example that, if M is an NFA that recognizes language C , swapping the accept and nonaccept states in M doesn't necessarily yield a new NFA that recognizes the complement of C . Is the class of languages recognized by NFAs closed under complement? Explain your answer.
- (Exercise 1.16; 20 points) Use the construction given in Theorem 1.39 (every NFA has an equivalent DFA) to convert the following NFA into an equivalent DFA.



4. (Exercise 1.18; 10 points) Use the procedure described in Lemma 1.55 to convert the regular expression $(0 \cup 1)^+ 011(0 \cup 1)^*$ into an NFA.
5. (Exercise 1.20; 10 points) Give regular expressions generating the following languages:
 - (a) $\{w \mid w \text{ contains the substring } 0101, \text{ i.e., } w = x0101y \text{ for some } x \text{ and } y\}$
 - (b) $\{w \mid w \text{ doesn't contain the substring } 011\}$
6. (Exercise 1.21; 20 points) Use the procedure described in Lemma 1.60 to convert the following finite automaton into a regular expression.



7. (Exercise 1.24; 10 points) A *finite-state transducer* (FST) is a type of deterministic finite automaton whose output is a string rather than *accept* or *reject*. The following are state diagrams of finite state transducers T_1 and T_2 .



Each transition of an FST is labeled with two symbols, one designating the input symbol for that transition and the other designating the output symbol. The two symbols are written with a slash, /, separating them. In T_1 , the transition from q_1 to q_2 has input symbol 2 and output symbol 1. Some conditions may have multiple input-output pairs, such as the transition in T_1 from q_1 to itself. When an FST computes on an input string w , it takes the input symbols $w_1 \cdots w_n$ one by one and, starting from the start state, follows the transitions by matching the input labels with the sequence of symbols $w_1 \cdots w_n = w$. Every time it goes along a transition, it outputs the corresponding output symbol. For example, on input 2212011, machine T_1 enters the sequence of states $q_1, q_2, q_2, q_2, q_2, q_1, q_1, q_1$ and produces output 1111000. On input $abbb$, T_2 outputs 1011. Give the sequence of states entered and the output produced in each of the following parts.

- (a) T_1 on input 122021
 - (b) T_2 on input baaabb
8. (Exercise 1.25; 10 points) Read the informal definition of the finite state transducer given in Exercise 1.24. Give a formal definition of this model, following the patterns in Definition 1.5 (Page 35 in Sipser's book or Page 7 of the slides). Assume that an FST has an input alphabet Σ and an output alphabet Γ but not a set of accept states. Include a formal definition of the computation of an FST. (Hint: an FST is a 5-tuple. Its transition function is of the form $\delta : Q \times \Sigma \rightarrow Q \times \Gamma$.)