Homework Assignment #6

Due Time/Date

2:20PM Wednesday, December 6, 2023. Late submission will be penalized by 20% for each working day overdue.

How to Submit

This assignment must be carried out using Coq and Frama-C. Please email your completed homework in one single .zip file to the instructor by the due time. You may discuss the problems with others, but copying answers is strictly forbidden.

Problems

(30 points) Prove the following lemmas using Coq. The predicate Zis_gcd in Lemma gcd_equiv is defined in the ZArith.Znumtheory library such that Zis_gcd a b d asserts that d is the GCD of a and b. (Hint: for constructing the proofs, most needed lemmas may be found in the ZArith.BinInt library.)

2. (30 points) Annotate the following C function to show that it preserves sortedness of the input array (i.e., the input array remains sorted if it was sorted), assuming no underflow will occur, and prove correctness of your annotation using Frama-C.

```
void add1(int* a, int n) {
    int i;
    for (i=n-1; i>=0; i--)
        a[i]--;
}
```

3. (40 points) Annotate the following C function to show its behavior and prove correctness of your annotation using Frama-C.

```
int originalEuclid(int m, int n)
{ int x,y,tmp;
    x = m;
    y = n;
    while (x != y) {
        if (x < y) {
            tmp = x;
            x = y;
            y = tmp;
        }
        x = x - y;
    }
    return x;
}</pre>
```